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# The effects of Si substitution on the glass forming ability of Ni–Pd–P system, a DFT study on crystalline related clusters



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# ABSTRACT

In order to investigate the influence of Si in the glass forming ability of Pd–Ni–P based bulk metallic glasses, the topological and electronic structure of stoichiometry related crystals is explored using density functional theory. The results indicate that Si based clusters based on a rich Pd environment with a symmetric configuration of the transition metal are the most stable, while P prefers a Ni rich environment with an asymmetric arrangement of the transition metals. Si tends to be at the center of the clusters, while in general the P atoms present a displacement toward some of the Ni atoms. The coordination of Si in rich Ni crystals is always higher than the one observed for P atoms. Also, the inclusion of Si induces a local pressure field in a radius of 14 Å leading to a disordered displacement of P from the equilibrium positions. The favoring of different competing crystals by adding Si, as well as the local pressure effect, suggests a mechanism on how devirtification is suppressed.

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## 1. Introduction

The metallic amorphous alloys have been attracting much attention due to their unusual properties comparing with their crystalline phases. Such potential properties are, for example, corrosion resistance, temperature-insensitive electrical conductivity, ductility, and high strength [1]. Nowadays there are several bulk metallic glass (BMG) systems, although it is not clear so far the physical origin of this glass formation [2]. The history of BMG started with the  $Au_{75}Si_{25}$ alloy, that was first reported by Klement et al. in 1960 [3]. Then Pd-based metallic alloys were made by rapid melt quenching. With this method. Chen prepared millimeter-diameter rods of Pd-Cu-Si BMG [4]. Using the Pd-based BMG. Drehman et al. prepared the famous Pd-Ni-P BMG [5,6]. They used boron oxide fluxing method to prevent heterogeneous nucleation. One fact that limits the Pd-based BMG mass production is the high cost of the Pd metal, therefore it was necessary to search new metal-based BMG compositions. Inoue and coworkers had found new multicomponent BMGs with excellent glass-formation ability (GFA) [7], for example: Mg-, Ln-Zr-, Fe-, Pd-Cu-, Pd-Fe-, Ti- and Ni-based alloy systems. In this context, Pd<sub>40</sub>Ni<sub>10</sub>Cu<sub>Cu</sub>P<sub>20</sub> and Pd<sub>42.5</sub>Ni<sub>7.5</sub>Cu<sub>30</sub>P<sub>20</sub> have the lowest critical cooling rate of 0.10 and 0.067 K/s, which can be associated to the best GFA [8,9].

Several criteria for determining GFA have been proposed, for example, the reduced glass transition temperature  $T_{rg}$ , proposed by Turnbull [10], which corresponds to the ratio of the glass transition temperature  $(T_g)$  to the melting point  $(T_m)$  of alloy. Also, the criteria  $1/(T_g + T_l)$  and  $T_x$  can be used, where  $T_g$ ,  $T_l$  and  $T_x$  are the glass transition, the liquidus

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and the onset crystallization temperatures, respectively [11]. Experimentally, one factor that spoils the glass-formation abilities is the small oxide particles within the melt, this limitation can be improved by fluxing  $B_2O_3$  [6]. The crystallization in  $Pd_{40}Ni_{40}P_{20}$  can be either from internal nuclei or from surface impurities, therefore heterogeneous nucleation is an important limitation on the GFA [12–14].

It was reported that, with a minor addition of Si, Pd–Ni–P and Cu–Hf–Ti BMGs had significantly improved of the GFA [15–17]. In the cases of  $Pd_{40}Ni_{40}P_{20}$  and  $Pd_{20}Ni_{60}P_{20}$  systems, it is not clear why only with the small addition of Si (4% and 2%),  $\Delta T_x = T_x - T_g$  reached a maximum (120 and 74 K). Zeng et al. pointed out that with this percent, the heterogeneous crystallization was suppressed. It is important to remark that with a higher Si content the GFA is decreased.

In this work, we discuss the influence of the trigonal prism cluster units with P occupying the center site. Also, we focus on the substitution of P by Si in Pd–Ni–P systems. To do this, we studied several related crystalline phases in which is known that the same clusters observed in the glass appear [18].

Our main results indicate that Si tends to promote completing crystals favoring the formation of glass. Also, Si produces a kind of shoving effect by inducing a local internal pressure field in a radius of 14 Å which interferes with the off-center P displacement inside clusters. The different connectivity of the network can help to explain the improved mechanical properties as explained by J.C. Phillips rigidity theory [19–26].

The layout of this work is the following. We start with the description of the Pd–Ni–P and Pd–Ni–Si crystals and methods used. Then the structural effects of the Si inclusion are analyzed, which are followed by the study of the electronic properties. Finally, the conclusions are given.

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#### Table 1

Crystallographic details of the Ni-P, Pd-Ni-P, Pd-P and Pd-Ni-Si systems [27,28].

Empirical formula	Space group	a (Å)	b (Å)	c (Å)
Ni <sub>2</sub> P	P <del>6</del> 2m	5.87	5.87	3.39
PdNiP	P62m	6.02	6.02	3.60
Pd₃ P	Pnma	5.70	7.54	5.12
PdNi <sub>2</sub> P	Cmcm	3.47	8.44	6.61
PdNiSi	P62m	6.27	6.27	3.35

#### 2. Materials and methods

We have decided to focus on the Pd–Ni–P systems by studying the related crystalline structures: Ni<sub>2</sub>P, PdNiP, PdNi<sub>2</sub>P, Pd<sub>3</sub>P and by systematically replacing P by Si in several compounds. Also, the PdNiSi and PdNi<sub>2</sub> Si crystals were studied. The corresponding crystallographic structures were obtained from references [27,28] and detailed in Table 1. All the corresponding structures were relaxed using usual atomic simulation techniques based on density functional theory (DFT).

These ab initio calculations were done by using the Quantum ESPRESSO [29] plane wave DFT and density functional perturbation theory (DFPT) code, available under the GNU Public License [30].

Scalar relativistic and non-spin polarized calculation were performed. A plane-wave basis set with the cutoff of 612 eV was used. Also, an ultrasoft pseudo-potential [31] from the standard distribution generated using a modified RRKJ [32] approach, and the generalized gradient approximation [33] (GGA) for the exchange-correlation functional in its PBE parametrization [34] was used. All atomic positions and lattice parameters of the supercells were optimized using the conjugate gradient method. The convergence for energy was chosen as  $10^{-7}$  eV between two consecutive

steps and the maximum forces acting are smaller than 0.05 eV/Å. The stress in the periodic direction is lower than 0.01 GPa in all cases.

Of special importance is the PdNi<sub>2</sub>P crystal, which is the closest one to the Pd<sub>20</sub>Ni<sub>60</sub>P<sub>20</sub> experimentally studied glass [16]. The PdNi<sub>2</sub>P primitive cell is trigonal with a = 4.8761 Å and c = 6.6081 Å ( $\rho = 8.74$  gr/cm<sup>3</sup>) [28]. This primitive cell was grown from 8 atoms to supercells of 16, 32, 64 and 128 atoms.

As the supercell grows, the % Si concentration can be decreased in order to achieve the goal of a small P substitution. Si was put in the following concentrations:  $Pd_2Ni_4(P_1Si_1)$  (25% Si),  $Pd_4Ni_8(P_3Si_1)$  (6.25% Si),  $Pd_8Ni_{16}(P_8Si_1)$  (3.13% Si),  $Pd_{16}Ni_{32}(P_{15}Si_1)$  (1.6% Si), and  $Pd_{32}Ni_{64}(P_{31}Si_1)$  (0.8% Si). The corresponding structural and electronic properties are described in the following sections.

## 3. Results and discussion

#### 3.1. Structural properties

The basic building block of Pd–Ni–P systems is based on trigonal prisms, with a P at the center of the prisms [7,18]. Six transition metals (TM) are in the corners of the prisms while three other TM are in the faces, as detailed in Fig. 1.

Several interesting features were obtained after the system relaxation,

- 1) Observations in pure Pd-Ni-P systems
- As the basic crystal PdNiP is enriched with Ni, the relaxation of Pd– Ni–P systems shows that P tends to move slightly away from the center of the trigonal prisms, see Fig. 2. The reason is that in PdNiP, there are three Pd in the faces of the trigonal prism, as indicated in Fig. 1. However, as Ni replaces Pd, the TM are not placed



**Fig. 1.** The building blocks of PdNiP (1-a and 1-c) and PdNi<sub>2</sub>P (1-b and 1-d) with different ball sizes and orientations. Notice in (d) the small displacement of the P atom from the center of the trigonal prism in PdNi<sub>2</sub>P, and how this results in two P – Pd broken bonds in (b). Gray, blue and yellow balls represent palladium, nickel and phosphorus, respectively. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



**Fig. 2.** Central P viewed from the top of the trigonal prism in 2-a PdNiP and 2-b PdNi<sub>2</sub>P. In inset 2-c, we present a schematic cut of the prism. The dashed line corresponds to a P - Pd broken bond, while the arrow indicates the movement performed by the P atom from the center as Ni is added. The same color code of Fig. 1 is used. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

symmetrically in the plane that cuts the trigonal prism at the middle. As a result, P tends to stick with the Ni, and the two distances from Pd increase from 2.43 to 2.54 Å and one decreases from 2.43 to 2.41 Å, bringing as a consequence two broken P–Pd bonds and one stronger P–Pd bonds, respectively. The local structure of the P centered cluster and the corresponding distances between atoms are detailed in Fig. 1 and Table 2. A good agreement is found with the experimental observed values. The movement of the central P is correlated with changes in the electronic structure, as will be discussed later on.

We have tested several pressures in order to study the effects upon the central P movement in PdNi<sub>2</sub>P. By applying 100 K bars, P returns to the center of the clusters.

2) Inclusion of Si on Pd-Ni-P

Contrasting with the previous behavior, when P is gradually replaced by Si at the center of the clusters, the local environment around Si is almost the same for all compositions, preserving all the bonds as seen in Fig. 3. As a consequence, the coordination of

#### Table 2

Distances inside the building block for PdNiP, PdNi <sub>2</sub> P, PdNiSi and PdNi <sub>2</sub> Si as obtained fro
DFT. The values in parentheses are the experimental values [27,28].

System PdNiP dis	stances	PdNi <sub>2</sub> P distances
P–Ni P–Pd Pd–Ni	2.38 (2.37) Å 2.43 (2.45) Å 2.80 (2.80) Å	2.24 (2.26) and 2.28 (2.29) Å 2.41 (2.42) and 2.54 (2.50) Å 2.76 (2.76) and 2.84 (2.85) Å
System PdNiSi di	stances	PdNi <sub>2</sub> Si distances

Si is *always the same as* P in the crystal PdNiP. Thus, this is a clear indication that Si tends to stabilize the clusters based on the trigonal prism even for an asymmetric distribution of TM. Also, Si has another important effect on the surrounding P based clusters. Since Si is bigger than P, the edges of the trigonal prism are increased as indicated in Table 2. We have found that this induces a local internal pressure that tends to move neighboring P atoms from its equilibrium value. This behavior is a kind of shoving [35,36], where the local cluster expansion around Si leads to a domino effect that propagates along the system. One can speculate that this helps to increase the GFA with only a 1% or 2% of Si.

To test the previous hypothesis, one can extract from the simulations the characteristic length of the Si influence. Thus, we calculated the ratios between the distances from P to each kind of non-equivalent TM as a function of the P atom distance from the Si. This allows to detect which bonds tend to be broken as the P moves from the center of the cluster as a function of the distance from the Si. Two kinds of ratios are defined. If we define  $d_{\rm TM}^t$  as the distance from P to the TM on the faces and  $d_{\rm PTM}^t$  as the distance from P to the prisms, then the ratio  $d_{\rm P}^f - Ni/d_{\rm P}^f - Pd$  measures the displacement of P from the equilibrium position defined in Fig. 1, while  $d_{\rm P}^{\rm P} - Ni}/d_{\rm P}^{\rm P} - Pd}$  captures a displacement that involves the vertical axis of Fig. 1.

In Fig. 4 one can see the effect of the Si inclusion in the compound  $Pd_{32}Ni_{64}P_{31}Si_1$  in a cell of 128. This compound has been chosen because it has the lowest proportion of Si. As a result, one can estimate the influence length of the inclusion. From Fig. 4 it is clear that such length is around 14 Å. This length is consistent with the idea of having at least a 1% or 2% of Si, since if we want to cover all the P atoms in the system inside non-intersecting 14 Å spheres centered in Si, the result turns out to be around  $\approx 1.2\%$ . For smaller Si concentrations, some P-based clusters are too far away to be affected, while too much Si leads to overlapping spheres in which Si based crystals can grow. (See Fig. 3.)



**Fig. 3.** Insets 3-a and 3-c correspond to the same PdNiSi crystalline cluster viewed in two different orientations around the Si atom. Insets 3-b and 3-d correspond to different views of the same cluster around the Si atom for the supercell Pd<sub>32</sub>Ni<sub>64</sub>P<sub>31</sub>Si<sub>1</sub>.



**Fig. 4.** Distances ratios of P from a Si inclusion in a cell of 128 atoms in the compound Pd<sub>32</sub>Ni<sub>64</sub>P<sub>31</sub>Si<sub>1</sub>. In inset 4-a,  $d_P^{f} - _{Ni}$  and  $d_{P}^{f} - _{Pd}$  are the distances from the central P to the Ni and Pd situated on the faces of the trigonal prisms. In inset 4-b,  $d_{P}^{fP} - _{Ni}$  and  $d_{P}^{fP} - _{Pd}$  are the distances from the central P to the Ni and Pd situated on the corners of the trigonal prisms, see Fig. 1. The arrow indicates the maximal radius of the perturbation.

This suggests an idea on how Si has an influence on the devitrification dynamics, which is a complex process of crystallite nucleation and phase separation [19–25]. This complex process can be represented by paths in a high-dimensional phase space [37–39]. Along these paths, the off-center P displacement has a knock-on effect (domino effect), with each successive off-center P displacement pushing the next offcenter P displacement, and so on resulting in an internal stress transmission. Introducing a small amount of Si interrupts this process. The local pressure and strain induced by Si also can have an impact in the glass transition temperature through the vibrational properties of the glass by increasing its local connectivity [26,40–43].

#### 3.2. Electronic properties

In Fig. 5 we present a comparison between the DOS of PdNiP and PdNi<sub>2</sub>P. For PdNiP, the DOS is higher at the fermi energy ( $E_F$ ) than for PdNi<sub>2</sub>P. This suggests that PdNi<sub>2</sub>P crystal is more stable, as is also reflected in the cohesive energies, see Table 3. This fact is well supported by a recent study of atomic tomography of crystalline and amorphous Pd–Ni–P



Fig. 5. Comparison of the electronic density of states for PdNiP and PdNi<sub>2</sub>P crystals. The Fermi energy is marked with a vertical red line and has been set to zero. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

system [14]. It has been found that heterogeneous microcrystals were basically made of PdNi<sub>2</sub>P, while glasses tended to be richer in Pd.

From Figs. 5 to 9, we provide an overall picture of the substitution effects of P by Si in the electronic structure of the relaxed related crystals. There are two noticeable features,1) As seen in Figs. 5, 7 and 9, a small bump appears at -10 eV below the E<sub>F</sub> when Si is added. At the same time, the bump around -15 eV decreases. Such effect is easily explained by looking at the band structure. In the partial DOS (pDOS) on each kind of atom, the bump at -15 eV is due to valence 3s states of P, while the bump at -10 eV is due to the Si 3s states, see for example cases PdNiP and PdNiSi pDOS of Figs. 6 and 8 respectively.

Also, from the partial DOS, an important feature that we found is that the *s* states in Si are much more hybridized with the *d* states of the transition metals (TM). This means that s states have a more important role in the bonding, as is reflected in the cohesion energy of the systems (see Table 3). The effect of Si is to increase the cohesion energy.

It is important to remark that the hybridized bands of p states of Si and P with the d bands of the TM are similar in energy, around -5 eV. The Si p-d hybridized orbitals tend to lie in a slightly higher energy, so the main reason for the increased cohesion is the hybridization of s orbitals of Si when compared with P.

2) For PdNiP,  $E_F$  falls near a peak, as seen in Fig. 7. In this compound, a few percentage substitution of Si tends to move  $E_F$  to the bottom of a nearby pseudogap, indicating a tendency for cluster stabilization. If P is completely replaced by Si,  $E_F$  lies very close to the bottom of a deep pseudogap, as seen in Fig. 7. On the other hand, for PdNi<sub>2</sub>Si, the DOS is bigger at  $E_F$  in Fig. 7 and has less cohesion than in PdNiSi, as seen in Table 3.

For  $Pd_{20}Ni_{60}P_{20}$  related systems,  $E_F$  is close to a plateau in the DOS. The inclusion of a small percentage of Si increases the tendency of  $E_F$ 

Table 3

Cohesive energies for Pd–Ni–P, Pd–Ni–Si systems and the supercells with the Si inclusion in cells of 8, 16, 32, 64 and 128 atoms.

System	(eV/atom)	System	(eV/atom)				
PdNiP	5.2636	PdNiSi	5.4270				
PdNi <sub>2</sub> P	5.4213	PdNi <sub>2</sub> Si	5.4173				
Si inclusion in variable cells							
Pd <sub>2</sub> Ni <sub>4</sub> P <sub>2</sub>	5.4213	Pd <sub>2</sub> Ni <sub>4</sub> P <sub>1</sub> Si <sub>1</sub>	5.4219				
Pd <sub>4</sub> Ni <sub>4</sub> P <sub>4</sub>	5.4211	Pd <sub>4</sub> Ni <sub>8</sub> P <sub>3</sub> Si <sub>1</sub>	5.4221				
Pd <sub>8</sub> Ni <sub>16</sub> P <sub>8</sub>	5.4341	Pd <sub>4</sub> Ni <sub>16</sub> P <sub>7</sub> Si <sub>1</sub>	5.4345				
Pd <sub>16</sub> Ni <sub>32</sub> P <sub>16</sub>	5.4314	Pd16Ni32P15Si1	5.4324				
Pd <sub>328</sub> Ni <sub>64</sub> P <sub>32</sub>	5.4292	Pd <sub>32</sub> Ni <sub>64</sub> P <sub>31</sub> Si <sub>1</sub>	5.4293				



Fig. 6. Partial density of states at different local atomic environments for PdNiP after variable cell relax. The Fermi energy is marked with a vertical red line, and has been set to zero. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

to move near the minimum in all compounds. However, at equal percentages of Si and P, the DOS increases at E<sub>F</sub>, a fact that may explain why too much Si is also bad for glass forming ability (GFA) in PdNi<sub>2</sub>P.

The fact that DOS is a local maximum at  $E_{\rm F}$  in PdNiP and has less cohesion when compared with PdNi\_P needs to be contrasted with the



**Fig. 7.** Comparison of the electronic density of states for PdNiP, PdNiSi and PdNi<sub>2</sub>Si crystals. The Fermi energy is marked with a vertical red line, and has been set to zero. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

opposite behavior of Si. A deep pseudogap appears at  $E_F$  for PdNiSi and the system has a higher cohesion than in PdNi<sub>2</sub>P. Thus, Si favors Pd rich phases with a symmetric configuration of the transition metal at the faces of the trigonal prisms, while P favors Ni rich with an asymmetric configuration. This means that Si can enhance several competing crystals which eventually help to inhibit devitrification.

# 4. Conclusions

In conclusion, the structural and electronic effects of Si addition in Pd-Ni-P systems were analyzed. Under the assumption that Si replaces P inside the center of trigonal pyramids, we obtained that Si prefers clusters based on a rich Pd environment with a symmetric configuration of the transition metal at the faces, while P prefers a Ni rich environment with an asymmetric arrangement of the transition metals. Also, Si tends to be at the center of the clusters, while P presents a displacement towards some of the Ni atoms. As a result, in general the coordination of Si is higher than the one observed for P atoms. These observations help to understand why Si improves the GFA, since Si favors the formation of different competing crystalline phases. Furthermore, the inclusion of Si leads to a local expansion of the cluster, inducing a local pressure field around surrounding P clusters, which promotes disorder in the positions and coordination of the P-based clusters. The radius of influence of such "shoving effect" is around 14 Å, which explains in a rough way the experimental finding that a 1% or 2% of Si increases the glass forming ability.

The present work suggests that devitrification can be understood as complex cooperative phenomena, in which each successive off-center P displacement inside the basic cluster pushes the next off-center P displacement, favoring crystallization. It seems that a small amount of Si



Fig. 8. Partial density of states at different local atomic environments for PdNiSi after variable cell relax. The Fermi energy is marked with a vertical red line, and has been set to zero. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

interrupts this cooperative phenomenon. The local pressure and increased rigidity of the lattice induced by Si can also have an impact in the glass transition temperature and rheology [26,40–43]. Some of these interesting questions will be the subject of future works.

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Fig. 9. The electronic density of states for  $PdNi_2(P_1 - \chi Si)$ . Inset 9-b is a blow-up around  $E_F$ of the inset 9-a.

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